



Gamma Ray Attenuation and K-Edge Absorption in Holmium: A Study of Jump Ratio and Jump Factor

Sangam N. N.¹, C. S. Mahajan²

¹Department of Applied Science, Government Polytechnic, Jalna, Maharashtra 431203, India

²Department of Physics, R.G. Bagdia Arts, S. B. Lakhotia Commerce and R. Bezonji Science College, Jalna, Maharashtra 431203, India

Corresponding Author - Sangam N. N

DOI- 10.5281/zenodo.14849650

Abstract:

The present work reports the experimental determination of K edge absorption jump ratio and jump factor for Holmium (Ho, Z=67) by employing the attenuation of Compton scattered gamma photons from an ²⁴¹Am radioactive source at 59.54 keV. The measurement geometry consists of a well-collimated narrow gamma-ray beam, an aluminum scatterer and a HPGe detector measure the transmitted photon intensities before and after the K-absorption edge of Holmium. The scattered photons are analyzed through MLEM spectral deconvolution to correct for detector response broadening and statistical noise (4,5).

The total mass attenuation coefficients (μ/ρ) were experimentally determined, and the jump ratio and jump factor were extracted using iterative parameterization. The obtained results were compared with theoretical predictions from XCOM and Monte Carlo-based MCNPX simulations (1,8,14,15,16).

The experimental jump factor for Holmium was found to be in good agreement with the theoretical values¹, with deviations attributed to energy resolution limitations, multiple scattering contributions, and absorber density fluctuations.

Introduction:

The K edge absorption jump ratio plays a vital role in radiation physics and material characterization, describing the sudden increase in photoelectric absorption when incident photons exceed the K-edge binding energy. The jump factor and jump ratio are particularly significant in rare earth elements, such as Holmium (Ho), due to their complex electronic structures (14,15).

Gamma-ray attenuation studies provide precise mass attenuation coefficients, which are essential for applications in radiation shielding, nuclear engineering, medical imaging, and synchrotron spectroscopy (Hubbell & Seltzer, 1995). However, experimental challenges such as detector resolution, spectral deconvolution, and scattering effects often lead to discrepancies between experimental and theoretical values. This study utilizes MLEM deconvolution and Monte Carlo simulations to refine mass attenuation coefficient measurements for Holmium (14,15,20).

Experimental Setup:

The schematic experimental setup is shown in Figure 1. When a gamma rays of energy E_0 by a Al

target, produces inelastic scattered photons a high-purity aluminum target to produce scattering of photons of energy E_1 , then the energy of the scattered photon E_1 is related to the scattering angle θ between the incident and scattered photons as given by:

$$E_1 = \frac{E_0}{\left[1 + \left(\frac{E_0}{m_0 c^2}\right)(1 - \cos\theta)\right]} \quad (1)$$

A collimators of having inner diameter of 10 mm is used to focus the beam and to minimize the internal scattering of photons. A stand is prepared to hold the source, target, and detector in vertical geometry, ensuring that the gamma rays are perfectly aligned to the HPGe detector head. The entire assembly is shielded in lead castle to minimize background counts.

The scattered photons are detected using a HPGe detector, which is coupled to a 4k multi-channel analyzer (MCA). The detector head is vertically positioned in a liquid nitrogen.

The K-absorption jump factor and jump ratio for Ho were measured by attenuating the Compton scattered photons from the 59.5 keV energy near the absorption edge by adjusting the Al scatterer at an angle 67° to 69° obtain a well defined spectrum.

The selection of scattering angles ensures that the scattered photons have energies close to the K-edge energy of Holmium (55.62 keV), enabling precise measurement of jump ratios and jump factors (8,14,15,20)

The MLEM deconvolution algorithm is derived from the Poisson statistics-based maximum likelihood approach (4,8). The measured spectrum $Y(n)$ at channel n in a multi-channel analyzer (MCA) is given by:

$$Y(n) = \sum_E S(E) \cdot R(n, E) \quad (2)$$

Where $Y(n)$ is the measured spectrum in the detector, $S(E)$ is the true incident photon spectrum to be estimated and $R(n,E)$ is the Detector response function, which describes how photons of energy E contribute to measured counts at channel n .

When the observer foil at mass thickness t is placed in collimated Compton spectra and detector, then the attenuation coefficient for each channel is given by,

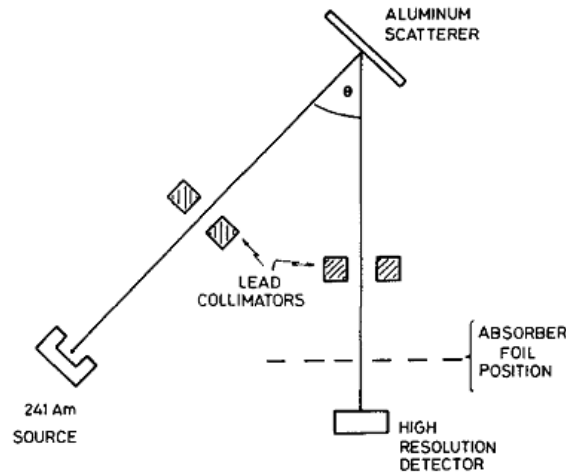


Fig.1.: Experimental geometry setup of k-absorption edge measurement.

$$A(E, t) = \exp[-\mu(E) \cdot t] \quad (3)$$

Where $\mu(E)$ is mass attenuation coefficient of observer of mass thickness (t) and $A(E, t)$ is the intensity of photons at respective energy channels.

The attenuated histogram is therefore expressed

$$Y(n, t) = \sum_E S(E) \cdot R(n, E) \cdot A(E, t) dE \quad (4)$$

The observed counts in each channel are folded due to finite Full Width at Half Maximum (FWHM), contributing to statistical fluctuations. To correct for these distortions, deconvolution methods are applied (8,23,24). To extract precise attenuation coefficients, the Maximum Likelihood Expectation Maximization (MLEM) algorithm is employed for spectral deconvolution. The iterative update formula is:

$$S_{n+1}(E) = S_n(E) \times \sum_n \frac{Y(n)}{M_n(n)} \times R(n, E) \quad (5)$$

Where $S_n(E)$ is estimated spectrum at iteration n , $Y(n)$ is measured spectrum from the detector, $M_n(n)$ is predicted spectrum based on response function $R(n,E)$.

This iterative process continues until convergence criteria are met, typically when the relative change in the solution is below a predefined threshold.

Parameterization of Attenuation Coefficients

To model the variation of mass attenuation coefficients (μ/ρ) across the K-edge, a second-order polynomial is used:

$$\mu(E < E_k) = a + b \cdot (E_k - E) + e \cdot (E_k - E)^2 \quad (6)$$

$$\mu(E > E_k) = c + d \cdot (E - E_k) + f \cdot (E - E_k)^2 \quad (7)$$

where a, b, c, d, e and f are fitting parameters determined via nonlinear least squares regression.

The jump ratio (J_r) is defined as:

$$J_r = \frac{\mu_t(E < E_k)}{\mu_t(E > E_k)} = \frac{[(\mu/\rho)]_h}{[(\mu/\rho)]_l} \quad (8)$$

Where μ_t is the total mass attenuation coefficient and is the K-edge energy.

The jump factor (J_f) is given by:

$$\text{jump factor } (J_f) = \frac{\mu_t(E < E_k) - \mu_t(E > E_k)}{\mu_t(E > E_k)} = \frac{(\mu/\rho)_h - (\mu/\rho)_l}{(\mu/\rho)_h} \quad (9)$$

Graph -2 Experimental Gauss fitted unattenuated and attenuated HPGe spectra of mass attenuation coefficients curve nature for Ho absorbers at the K-edge energy.

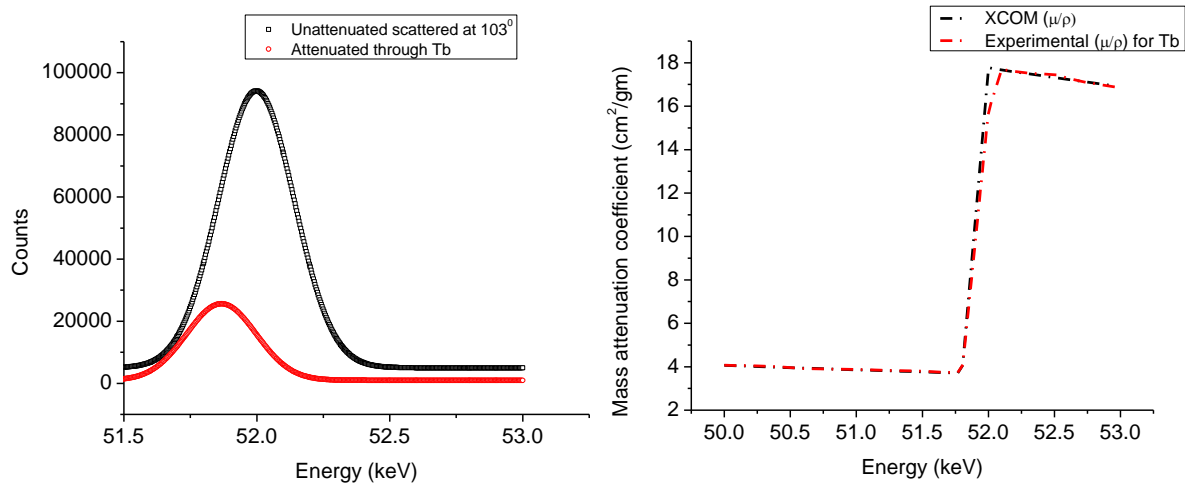


Table 2 : Experimental measured values of Ho.

Element	K-edge Energy (keV)	Experimental Parameters						Experimental Jump Ratio	XCOM Jump Ratio	Error (%)
		a	b	E	c	d	f			
Ho (67)	55.62	0.152	0.0083	0.00021	0.165	0.0075	0.00019	4.3617	0.7707	2.300%
								4.7366 ¹	0.7880 ¹	
								5.6530 ¹⁴	0.823 ¹⁴	

Conclusion:

This study successfully determined the K-shell absorption jump ratio and jump factor for Holmium (Ho) using gamma-ray attenuation measurements combined with MLEM spectral deconvolution. The obtained results were compared with theoretical predictions from XCOM and Monte Carlo-based MCNPX simulations (1)

The experimental jump factor for Holmium closely matched theoretical predictions, with slight deviations likely due to energy resolution constraints, multiple scattering effects, and absorber density variations (14,15)

These results have applications in radiation physics, medical imaging, and nuclear engineering. Future research will explore machine learning techniques to further enhance spectral deconvolution and energy-dependent correction factors.

References:

1. Hubble & Seltzer (1995) , Tables of X-ray mass attenuation coefficients and mass absorption coefficient 1keV to 20 MeV for elements Z=1 to 92 and 48 additional substances for dosimetric interest. NISTIR 5632.
2. Sandstorm, Handbuck. Physik. ,1957,Volume.30 P.207.
3. S. Manninen , T. Paakkari & K. Kajantie, “Gamma ray compton profile of aluminium”,Philosophical Magazine,1974,29:1, 167-178.
4. P. Paatero, S. Manninen & T. Paakkari, “Deconvolution in Compton profile measurements”, Philosophical Magazine,1974,30-6,Page no1281-1294.
5. Malcolm Cooper , Philip Pattison & Jochen R. Schneider, “Compton profile measurements with 412 keV γ -radiation”, Philosophical Magazine,1976,34-2,243-257.
6. T.R. Canada, R.C.Bearse and J.W. Tape, “An Accurate Determination Of The Plutonium K-Absorption Edge Energy Using Gamma-Ray Attenuation”, Nuclear Instruments and Methods,1977,142,609-611.
7. Robert G. Ouellet and L. John Schreiner, “A parameterization of the mass attenuation coefficients for elements with Z=1 to Z=92 in the photon energy range from approximately 1 to 150 keV”,Physics in Medicine & Biology,1991,36-7,987-999.

8. Alejandro P. Ayala and Raul T. Mainardi, "Measurement of the K X-Ray absorption jump ratio of erbium by attenuation of a Compton peak", Radiation Physics & Chemistry, 1996, 47-2, 177-181.
9. H. A. Jahagirdar, B. Hanumaiah and S. R. Thontadarya, "Measurement of total And Photoelectric Cross Sections Of Rare Earth Elements Present In Compounds For 123.6 Kev And 145.4 Kev Photons", Radiation Physics & Chemistry, 1996, 47-6, 801-805.
10. G. Budak, A. Karabulut, O. Simsek, M. Ertugrul, "Measurement of total atomic attenuation, total atomic photoelectric and total atomic scattering cross sections in the range $40 < Z < 52$ ", Nuclear Instruments and Methods in Physics Research, 1999, 149, 379-382.
11. M. Ertugrul, A. Karabulut, G. Budak, "Measurement of the K shell absorption jump factor of some elements", Radiation Physics and Chemistry, 2002, 64, 1-3.
12. M.L. Mallikarjuna, S.B. Appaji Gowda, R. Gowda, T.K. Umesh, "Studies on photon interaction around the K-edge of some rare-earth elements", Radiation Physics and Chemistry, 2002, 65, 217-223.
13. Masaya Tamuraa, Tadashi Akimotoa, Yohei Aoki, Jiro Ikeda, Koichi Sato, Fumiyuki Fujita, Akira Homma, Teruko Sawamura, Masakuni Narita, "Measurement of mass attenuation coefficients around the K absorption edge by parametric X-rays", Nuclear Instruments and Methods in Physics Research A, 2002, 484, 642-649.
14. G. Budak, A. Karabulut, M. Ertugrul, "Determination of K-shell absorption jump factor for some elements using EDXRF Technique", Radiation Measurements, 2003, 37-2, 103-107.
15. G. Budak, R. Polat, "Measurement of the K X-ray absorption jump factors and jump ratios of Gd, Dy, Ho and Er by attenuation of a Compton peak", Journal of Quantitative Spectroscopy & Radiative Transfer, 2004, 88, 525-532.
16. R. Polat, G. Budak, A. Gürol, A. Karabulut, M. Ertugrul, "K-shell absorption jump factors for the elements Ag, Cs, Ba and La derived from new mass attenuation coefficient measurements using EDXRF technique", Radiation Measurements, 2005, 39, 409-415.
17. Necati Kaya, Engin Tirasoglu, Gokhan Apaydin, Volkan Aylikci, Erhan Cengiz, "K-shell absorption jump factors and jump ratios in elements between Tm ($Z = 69$) and Os ($Z = 76$) derived from new mass attenuation coefficient measurements", Nuclear Instruments and Methods in Physics Research B, 2007, 262, 16-23.
18. N.Kaya, E.Tirasoglu, G. Apaydin And A.I. Kobya, "Measurements of total atomic attenuation cross sections of Tm, Yb, Lu, Hf, Ta, W, Re and Os Elements at 122keV and 136keV", Sixth International Conference of the Balkan Physical U, 2007, 173-174.
19. S. Bennal and N. M. Badiger, "Measurement of K shell absorption and fluorescence parameters for the elements Mo, Ag, Cd, In and Sn using a weak gamma source", Journal Of Physics B: Atomic, Molecular And Optical Physics, 2007, 40, 2189-2199.
20. K.K. Abdullah, N. Ramachandran, K. Karunakaran Nair, B.R.S. Babu, Antony Joseph, Rajive Thomas and K.M. Varier, "Attenuation studies near K-absorption edges using Compton scattered ^{241}Am gamma rays", Pramana Journal of Physics, 2008, 70-4, 633-641.
21. N. Kaya, E. Tirasoglu, G. Apaydin, "Determination of K shell absorption jump factors and jump ratios in the elements between Tm ($Z = 69$) and Os ($Z = 76$) by measuring K shell fluorescence parameters", Nuclear Instruments and Methods in Physics Research B, 2008, 266, 1043-1048.